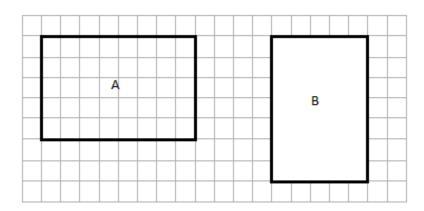
Name \_\_\_\_\_ Date \_\_\_\_\_

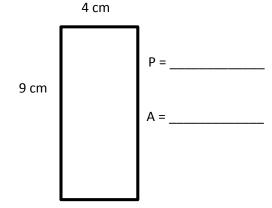
1. Determine the perimeter and area of rectangles A and B.



2. Determine the perimeter and area of each rectangle.

a.

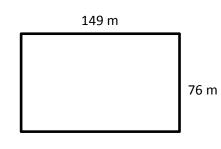
3 cm



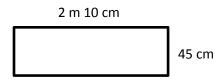


3. Determine the perimeter of each rectangle.

a.



b.

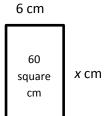


P = \_\_\_

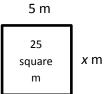
P = \_\_\_\_\_

4. Given the rectangle's area, find the unknown side length.

a.



b.



x = \_\_\_\_\_

x = \_\_\_\_\_

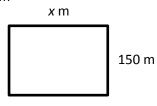
G4-M3-TE-1.3.0-06.2015

5. Given the rectangle's perimeter, find the unknown side length.

a. P = 180 cm

cm

b. P = 1,000 m



6. Each of the following rectangles has whole number side lengths. Given the area and perimeter, find the length and width.

a. A = 32 square cm

P = 24  cm	
------------	--

b. A = 36 square m

32 square cm

w = \_\_\_\_

w = \_\_\_\_

square

Na	me	Date
1.	A rectangular pool is 7 feet wide. It is 3 times as long as it is v	vide.
	a. Label the diagram with the dimensions of the pool.	
	b. Find the perimeter of the pool.	
2.	A poster is 3 inches long. It is 4 times as wide as it is long.	
	a. Draw a diagram of the poster, and label its dimensions.	
	b. Find the perimeter and area of the poster.	





	3.	The area of a	rectangle is 36 sq	uare centimeters.	, and its length	is 9 centimeters.
--	----	---------------	--------------------	-------------------	------------------	-------------------

a. What is the width of the rectangle?

b. Elsa wants to draw a second rectangle that is the same length but is 3 times as wide. Draw and label Elsa's second rectangle.

c. What is the perimeter of Elsa's second rectangle?

Lesson 2:



Solve multiplicative comparison word problems by applying the area and perimeter formulas.



4.	The area of Nathan's bedroom rug is 15 square feet. The longer side measures 5 feet. His living room rug
	is twice as long and twice as wide as the bedroom rug.

a. Draw and label a diagram of Nathan's bedroom rug. What is its perimeter?

b. Draw and label a diagram of Nathan's living room rug. What is its perimeter?

c. What is the relationship between the two perimeters?

d. Find the area of the living room rug using the formula  $A = I \times w$ .



Lesson 2:

Solve multiplicative comparison word problems by applying the area and perimeter formulas.



٩	The living room	rug has an	area that is how	w many times tha	at of the bedroom	rug?
С.	THE HVILLE TOOM	i i ug iias aii	area triat is not	w many united the	at of the beardonn	iug:

f. Compare how the perimeter changed with how the area changed between the two rugs. Explain what you notice using words, pictures, or numbers.



Lesson 2:

Solve multiplicative comparison word problems by applying the area and perimeter formulas.



Na	me Date
Sol	ve the following problems. Use pictures, numbers, or words to show your work.
1.	Katie cut out a rectangular piece of wrapping paper that was 2 times as long and 3 times as wide as the box that she was wrapping. The box was 5 inches long and 4 inches wide. What is the perimeter of the wrapping paper that Katie cut?
2.	Alexis has a rectangular piece of red paper that is 4 centimeters wide. Its length is twice its width. She glues a rectangular piece of blue paper on top of the red piece measuring 3 centimeters by 7 centimeters. How many square centimeters of red paper will be visible on top?



3.	Brinn's rectangular kitchen has an area of 81 square feet. The kitchen is 9 times as many square feet as
	Brinn's pantry. If the rectangular pantry is 3 feet wide, what is the length of the pantry?

4. The length of Marshall's rectangular poster is 2 times its width. If the perimeter is 24 inches, what is the area of the poster?



Lesson 3:

Demonstrate understanding of area and perimeter formulas by solving multi-step real-world problems.  $\textbf{engage}^{\textbf{ny}}$ 



Name \_\_\_\_\_

Date \_\_\_\_\_

Example:

$$5 \text{ ones} \times 10 = \frac{5}{100} \text{ tens}$$

thousands	hundreds	tens	ones
		<b>*10</b>	••••
		00000	

Draw place value disks and arrows as shown to represent each product.

thousands	hundreds	tens	ones

3. Fill in the blanks in the following equations.

$$f. \times 3 = 300$$

$$h = 10 \times 4$$



Lesson 4:

Interpret and represent patterns when multiplying by 10, 100, and 1,000 in arrays and numerically.

Draw place value disks and arrows to represent each product.

(1 ten 5 ones) × 10 = \_\_\_\_\_

thousands	hundreds	tens	ones

(1 ten 7 ones) × 100 = \_\_\_\_\_

thousands	hundreds	tens	ones

36 × 10 × 10 × 10 = \_\_\_\_\_

(3 tens 6 ones) × 1,000 = \_\_\_\_\_

thousands	hundreds	tens	ones
	thousands	thousands hundreds	thousands hundreds tens

Decompose each multiple of 10, 100, or 1000 before multiplying.

7. 
$$2 \times 80 = 2 \times 8 \times ____$$

= \_\_\_\_× \_\_\_\_



Lesson 4:

Interpret and represent patterns when multiplying by 10, 100, and 1,000 in arrays and numerically.



Name	Date
INGILIE	Date

Draw place value disks to represent the value of the following expressions.

1. 5 × 2 = \_\_\_\_\_

5 times \_\_\_\_\_ ones is \_\_\_\_\_ ones.

thousands	hundreds	tens	ones

2. 5 × 20 = \_\_\_\_\_

5 times \_\_\_\_\_\_ tens is \_\_\_\_\_\_.

hundreds	tens	ones
	hundreds	hundreds tens

2 × 5

3. 5 × 200 =

5 times \_\_\_\_\_ is \_\_\_\_\_

thousands	hundreds	tens	ones

4. 5 × 2,000 = \_\_\_\_

\_\_\_\_ times \_\_\_\_\_ is \_\_\_\_\_

thousands	hundreds	tens	ones



Lesson 5:

Multiply multiples of 10, 100, and 1,000 by single digits, recognizing patterns.



5. Find the product.

a.	20 × 9	b. 6×70	c. 7×700	d. 3 × 900
e.	9 × 90	f. 40 × 7	g. 600 × 6	h. 8 × 6,000
i.	5 × 70	j. 5 × 80	k. 5 × 200	I. 6,000 × 5

6. At the school cafeteria, each student who orders lunch gets 6 chicken nuggets. The cafeteria staff prepares enough for 300 kids. How many chicken nuggets does the cafeteria staff prepare altogether?

7.	Jaelynn has 30 times as many stickers as her brother.	Her brother has 8 stickers.	How many stickers does
	Jaelynn have?		

8. The flower shop has 40 times as many flowers in one cooler as Julia has in her bouquet. The cooler has 120 flowers. How many flowers are in Julia's bouquet?



Multiply multiples of 10, 100, and 1,000 by single digits, recognizing  $\,$ patterns.



Lesson 5:

Name	Date	

Represent the following problem by drawing disks in the place value chart.

1. To solve  $30 \times 60$ , think

hundreds	tens	ones

2. Draw an area model to represent  $30 \times 60$ .

3. Draw an area model to represent  $20 \times 20$ .



4.	Draw an	area	model	to re	present	40 ×	60
----	---------	------	-------	-------	---------	------	----

Rewrite each equation in unit form and solve.



10. To print a comic book, 50 pieces of paper are needed. How many pieces of paper are needed to print 40 comic books?



Lesson 6:

Multiply two-digit multiples of 10 by two-digit multiples of 10 with the  $\,$ area model.



Name	Date	

- 1. Represent the following expressions with disks, regrouping as necessary, writing a matching expression, and recording the partial products vertically.
  - a.  $3 \times 24$

tens	ones

b.  $3 \times 42$ 

tens	ones
	tens

c.  $4 \times 34$ 

hundreds	tens	ones

Lesson 7:

Use place value disks to represent two-digit by one-digit multiplication.

- 2. Represent the following expressions with disks, regrouping as necessary. To the right, record the partial products vertically.
  - a.  $4 \times 27$

tens	ones
	tens

b.  $5 \times 42$ 

hundreds	tens	ones

3. Cindy says she found a shortcut for doing multiplication problems. When she multiplies 3 × 24, she says, "3 × 4 is 12 ones, or 1 ten and 2 ones. Then, there's just 2 tens left in 24, so add it up, and you get 3 tens and 2 ones." Do you think Cindy's shortcut works? Explain your thinking in words, and justify your response using a model or partial products.

Lesson 7:

Use place value disks to represent two-digit by one-digit multiplication.

- 1. Represent the following expressions with disks, regrouping as necessary, writing a matching expression, and recording the partial products vertically as shown below.
  - a. 2 × 424

hundreds	tens	ones
• • • •	• •	• • • •

	4	2	4	
×			2	
				→ 2 × ones
				→ 2 ×
+				→×

b.  $3 \times 424$ 

hundreds	tens	ones

c.  $4 \times 1,424$ 

- 2. Represent the following expressions with disks, using either method shown in class, regrouping as necessary. To the right, record the partial products vertically.
  - a. 2 × 617

b.  $5 \times 642$ 

c.  $3 \times 3,034$ 



3.	Every day, Penelope jogs three laps around the playground to keep in shape.	The playground is
	rectangular with a width of 163 m and a length of 320 m.	

a. Find the total amount of meters in one lap.

b. Determine how many meters Penelope jogs in three laps.



Lesson 8:

Extend the use of place value disks to represent three- and four-digit by one-digit multiplication.



Name	Date	

1. Solve using each method.

Pa	rtial Products	Standard Algorithm
a.	4 6	4 6
	_x 2	<u>× 2</u>

P	artial Products	Standard Algorithm
b.	3 1 5	3 1 5
	<u>× 4</u>	<u>× 4</u>

2. Solve using the standard algorithm.

a.	2 3 2 × 4	b. 1 4 2 × 6	c. 3 1 4 × 7
d.	4 4 0 × 3	e. 5 0 7 × 8	f. 3 8 4 × 9

<ol><li>What is the product of 8 and 54</li></ol>	3.	What is	the	product	of 8	and	54?
---	----	---------	-----	---------	------	-----	-----

4. Isabel earned 350 points while she was playing Blasting Robot. Isabel's mom earned 3 times as many points as Isabel. How many points did Isabel's mom earn?

5. To get enough money to go on a field trip, every student in a club has to raise \$53 by selling chocolate bars. There are 9 students in the club. How much money does the club need to raise to go on the field trip?



6. Mr. Meyers wants to order 4 tablets for his classroom. Each tablet costs \$329. How much will all four tablets cost?

7. Amaya read 64 pages last week. Amaya's older brother, Rogelio, read twice as many pages in the same amount of time. Their big sister, Elianna, is in high school and read 4 times as many pages as Rogelio did. How many pages did Elianna read last week?



Nar	me	Date		
1.	Solve using the standard algorithm.			
	a. 3×41	b. 9 × 41		
	c. 7×143	d. 7×286		
	e. 4×2,048	f. 4×4,096		
	g. 8 × 4,096	h. 4 × 8,192		



2.	Robert's family brings six gallons of water for the players on the football team. If one gallon of water contains 128 fluid ounces, how many fluid ounces are in six gallons?
3.	It takes 687 Earth days for the planet Mars to revolve around the sun once. How many Earth days does it take Mars to revolve around the sun four times?
4.	Tammy buys a 4-gigabyte memory card for her camera. Dijonea buys a memory card with twice as much storage as Tammy's. One gigabyte is 1,024 megabytes. How many megabytes of storage does Dijonea have on her memory card?

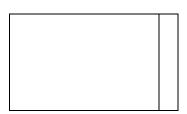


Name \_\_\_\_\_

Date \_\_\_\_\_

1. Solve the following expressions using the standard algorithm, the partial products method, and the area model.

a.  $302 \times 8$ 



8(300 + 2)

(8 × \_\_\_\_\_) + (8 × \_\_\_\_\_)

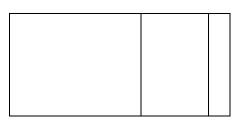
b.  $216 \times 5$ 



5 ( \_\_\_\_ + \_\_\_\_ + \_\_\_\_ )

(\_\_×\_\_\_)+(\_\_×\_\_\_)+(\_\_×\_\_\_)

c.  $593 \times 9$ 



\_\_(\_\_\_+\_\_\_+\_\_\_)

(\_\_×\_\_\_)+(\_\_×\_\_\_)+(\_\_×\_\_\_)

2.	Solve	using	the	partial	products	method.

On Monday, 475 people visited the museum. On Saturday, there were 4 times as many visitors as there were on Monday. How many people visited the museum on Saturday?

## 3. Model with a tape diagram and solve.

6 times as much as 384

Solve using the standard algorithm, the area model, the distributive property, or the partial products method.

4.  $6,253 \times 3$ 



г	7 + 1	00 0000		2 07
5.	/ 1111111111111111111111111111111111111	as many	as	3,073

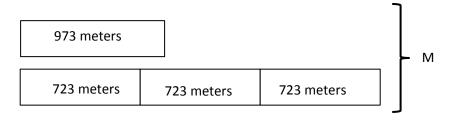
6. A cafeteria makes 2,516 pounds of white rice and 608 pounds of brown rice every month. After 6 months, how many pounds of rice does the cafeteria make?



Nar	ne	Date			
Use	Use the RDW process to solve the following problems.				
1.	The table shows the number of stickers of various types in Chrissy's new sticker book. Chrissy's six friends each own the same sticker book. How many stickers do Chrissy and her six	Type of Sticker	Number of Stickers		
		flowers	32		
	friends have altogether?	smiley faces	21		
		hearts	39		
2.	The small copier makes 437 copies each day. The large copier make How many copies does the large copier make each week?  Jared sold 194 Boy Scout chocolate bars. Matthew sold three times				
3.	fewer than Matthew. How many bars did Gary sell?	s as ilially as Jafeu.	Jai y Solu 297		



Write an equation that would allow someone to find the value of M. 4. a.



Write your own word problem to correspond to the tape diagram, and then solve.



Na	me	Date		
Sol	ve using the RDW process.			
1.	A pair of jeans costs \$89. A jean jacket costs twice as much. pairs of jeans?	What is the total cost of a jean jacket and 4		
2.	Sarah bought a shirt on sale for \$35. The original price of th bought a pair of shoes on sale for \$28. The original price of Together, how much money did the shirt and shoes cost before the shirt and shirt	the shoes was 5 times that amount.		





3.	All 3,000 seats in a theater are being replaced. So far, 5 sections of 136 seats and a sixth section
	containing 348 seats have been replaced. How many more seats do they still need to replace?

4. Computer Depot sold 762 reams of paper. Paper Palace sold 3 times as much paper as Computer Depot and 143 reams more than Office Supply Central. How many reams of paper were sold by all three stores combined?



IVa	ne	Date
Use	the RDW process to solve the following problems.	
1.	Linda makes booklets using 2 sheets of paper. She has 17 sheets of booklets can she make? Will she have any extra paper? How many	
2.	Linda uses thread to sew the booklets together. She cuts 6 inches of many booklets can she stitch with 50 inches of thread? Will she has stitching up the booklets? If so, how much?	
3.	Ms. Rochelle wants to put her 29 students into groups of 6. How m If she puts any remaining students in a smaller group, how many students in a smaller group, how many students in a smaller group.	



4. A trainer gives his horse, Caballo, 7 gallons of water every day from a 57-gallon container. How many days will Caballo receive his full portion of water from the container? On which number day will the trainer need to refill the container of water?

5. Meliza has 43 toy soldiers. She lines them up in rows of 5 to fight imaginary zombies. How many of these rows can she make? After making as many rows of 5 as she can, she puts the remaining soldiers in the last row. How many soldiers are in that row?

Seventy-eight students are separated into groups of 8 for a field trip. How many groups are there? The remaining students form a smaller group of how many students?



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Lesson 14:

Name \_\_\_\_\_ Date \_\_\_\_\_

Show division using an array.	Show division using an area model.
1. 24 ÷ 4  Quotient =  Remainder =	Can you show 24 ÷ 4 with one rectangle?
2. 25 ÷ 4	
Quotient = Remainder =	Can you show 25 ÷ 4 with one rectangle? Explain how you showed the remainder:

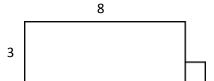
Solve using an array and area model. The first one is done for you.

Example:  $25 \div 3$ 

- a.

Quotient = 8 Remainder = 1

b.



3. 44 ÷ 7

a.

b.

4.  $34 \div 6$ 

a.

b.

5.  $37 \div 6$ 

a.

b.

6. 46 ÷ 8

a.

b.

Name Date
-----------

Show the division using disks. Relate your work on the place value chart to long division. Check your quotient and remainder by using multiplication and addition.

1. 7 ÷ 3

Ones		
	Ones	Ones

quotient =	
remainder =	

**Check Your Work** 

2

× 3

2.  $67 \div 3$ 

Tens	Ones

3 67

**Check Your Work** 

quotient = \_\_\_\_\_

remainder =

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Lesson 16:

Understand and solve two-digit dividend division problems with a remainder in the ones place by using place value disks.

3.  $5 \div 2$ 

Ones	

2 5

**Check Your Work** 

quotient = \_\_\_\_\_

remainder = \_\_\_\_\_

4.  $85 \div 2$ 

Tens	Ones
I	

2 85

quotient =
------------

remainder = \_\_\_\_\_

**Check Your Work** 



Lesson 16:

Understand and solve two-digit dividend division problems with a remainder in the ones place by using place value disks.



5.  $5 \div 4$ 

-	
	Ones
1	

4 5

quotient =	

remainder = \_\_\_\_\_

Check Your Work

6.  $85 \div 4$ 

Tens	Ones

4 85

quotient = _	

**Check Your Work** 

remainder = \_\_\_\_

engage<sup>ny</sup>



Lesson 16:

Understand and solve two-digit dividend division problems with a remainder in the ones place by using place value disks.

**Check Your Work** 

Name	Date
	Bate

Show the division using disks. Relate your model to long division. Check your quotient and remainder by using multiplication and addition.

1. 7 ÷ 2

Ones

2 7

quotient =	
remainder =	

2. 73 ÷ 2

Tens	Ones

2	7	3

Check Yo	our Work
----------	----------

3.  $6 \div 4$ 

	Ones
Ī	

4 6

**Check Your Work** 

quotient = \_\_\_\_\_

remainder = \_\_\_\_\_

4. 62 ÷ 4

Tens	Ones

4 6 2

quotient = \_\_\_\_\_

remainder = \_\_\_\_\_



Lesson 17:

Represent and solve division problems requiring decomposing a remainder in the tens.



**Check Your Work** 

5. 8 ÷ 3

1	Ones
•	

3 8

Check	Your	Work

quotient = \_\_\_\_\_

remainder = \_\_\_\_\_

6.  $84 \div 3$ 

Tens	Ones

3 8 4

	Check Your Work
quotient =	
remainder =	



Lesson 17:

Represent and solve division problems requiring decomposing a remainder in the tens.



Name	Date
Solve using the standard algorithm.	Check your quotient and remainder by using multiplication and addition

1. 84 ÷ 2	2. 84÷4
3. 48 ÷ 3	4. 80 ÷ 5
5. 79 ÷ 5	6. 91 ÷ 4



Lesson 18: Find whole number quotients and remainders.



7. 91 ÷ 6	8. 91 ÷ 7
0 07 : 3	10 07.6
9. 87 ÷ 3	10. 87 ÷ 6
11. 94 ÷ 8	12. 94 ÷ 6



Lesson 18: Find whole number quotients and remainders.

Name	Date	

1. When you divide 86 by 4, there is a remainder of 2. Model this problem with place value disks. In the place value disk model, how can you see that there is a remainder?

Francine says that  $86 \div 4$  is 20 with a remainder of 6. She reasons this is correct because  $(4 \times 20) + 6 = 86$ . What mistake has Francine made? Explain how she can correct her work.



 The place value disk model is showing 67 ÷ 4.
 Complete the model. Explain what happens to the 2 tens that are remaining in the tens column.

10 ho ho ho 10	
10	
10	
10	
10	

- 4. Two friends share 76 blueberries.
  - a. To count the blueberries, they put them into small bowls of 10 blueberries. Draw a picture to show how the blueberries can be shared equally. Will they have to split apart any of the bowls of 10 blueberries when they share them?

b. Explain how the friends can share the blueberries fairly.

Lesson 19:



Explain remainders by using place value understanding and models.



Imagine you are drawing a comic strip showing how to solve the problem  $72 \div 4$  to new fourth graders. Create a script to explain how you can keep dividing after getting a remainder of 3 tens in the first step.

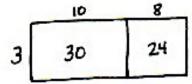


engage<sup>ny</sup> Explain remainders by using place value understanding and models.

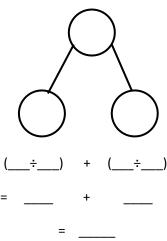
Lesson 19:

N.L	D. I.
Name	Date

- Maria solved a division problem by drawing an area model.
  - Look at the area model. What division problem did Maria solve?



Show a number bond to represent Maria's area model. Start with the total, and then show how the total is split into two parts. Below the two parts, represent the total length using the distributive property, and then solve.



2. Solve 42 ÷ 3 using an area model. Draw a number bond, and use the distributive property to solve for the unknown length.

Lesson 20:

3.	Solve 60 ÷ 4 using an area model. Draw a number bond to show how you partitioned the area, and
	represent the division with a written method.

4. Solve 72 ÷ 4 using an area model. Explain, using words, pictures, or numbers, the connection of the distributive property to the area model.

Solve 96 ÷ 6 using an area model and the standard algorithm.

Lesson 20:



Solve division problems without remainders using the area model.

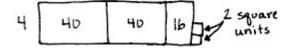


Name	Date
Name	Date

1. Solve  $35 \div 2$  using an area model. Use long division and the distributive property to record your work.

2. Solve  $79 \div 3$  using an area model. Use long division and the distributive property to record your work.

3. Paulina solved the following division problem by drawing an area model.



- a. What division problem did she solve?
- b. Show how Paulina's model can be represented using the distributive property.



Solve the following problems using the area model. Support the area model with long division or the distributive property.

4. 42 ÷ 3	5. 43 ÷ 3
6. 52 ÷ 4	7. 54 ÷ 4
8. 61 ÷ 5	9. 73÷3



Lesson 21:

Solve division problems with remainders using the area model.



10. Ninety-seven lunch trays were placed equally in 4 stacks. How many lunch trays were in each stack? How many lunch trays will be left over?



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Lesson 21:

Name	Date

1. Record the factors of the given numbers as multiplication sentences and as a list in order from least to greatest. Classify each as prime (P) or composite (C). The first problem is done for you.

	Multiplication Sentences	Factors	P or C
a.	8	The factors of 8 are:	С
	1 × 4 = 8 2 × 4 = 8	1, 2, 4, 8	
b.	10	The factors of 10 are:	
C.	11	The factors of 11 are:	
d.	14	The factors of 14 are:	
e.	17	The factors of 17 are:	
f.	20	The factors of 20 are:	
g.	22	The factors of 22 are:	
h.	23	The factors of 23 are:	
i.	25	The factors of 25 are:	
j.	26	The factors of 26 are:	
k.	27	The factors of 27 are:	
l.	28	The factors of 28 are:	



Lesson 22:

Find factor pairs for numbers to 100, and use understanding of factors to define prime and composite.



2. Find all factors for the following numbers, and classify each number as prime or composite. Explain your classification of each as prime or composite.

Factor Pairs for 21		Factor Pairs for 24	

- 3. Bryan says that only even numbers are composite.
  - a. List all of the odd numbers less than 20 in numerical order.
  - b. Use your list to show that Bryan's claim is false.
- 4. Julie has 27 grapes to divide evenly among 3 friends. She thinks there will be no leftovers. Use what you know about factor pairs to explain whether or not Julie is correct.



ne	Date
Explain your thinking or use division to a	answer the following.
a. Is 2 a factor of 72?	b. Is 2 a factor of 73?
c. Is 3 a factor of 72?	d. Is 2 a factor of 60?
e. Is 6 a factor of 72?	f. Is 4 a factor of 60?
g. Is 5 a factor of 72?	h. Is 8 a factor of 60?



Lesson 23:

Use division and the associative property to test for factors and observe patterns.



2. Use the associative property to find more factors of 12 and 30.

a. 
$$12 = 6 \times 2$$

3. In class, we used the associative property to show that when 6 is a factor, then 2 and 3 are factors, because  $6 = 2 \times 3$ . Use the fact that  $10 = 5 \times 2$  to show that 2 and 5 are factors of 70, 80, and 90.

$$70 = 10 \times 7$$

$$80 = 10 \times 8$$

$$90 = 10 \times 9$$

4. The first statement is false. The second statement is true. Explain why, using words, pictures, or numbers.

If a number has 2 and 6 as factors, then it has 12 as a factor.

If a number has 12 as a factor, then both 2 and 6 are factors.

Na	me	Date
1.	For each of the following, time yourself f	or 1 minute. See how many multiples you can write.
	a. Write the multiples of 5 starting from	n 75.
	b. Write the multiples of 4 starting from	n 40.
	c. Write the multiples of 6 starting from	n 24.
2.	List the numbers that have 30 as a multi	ole.
3.	Use mental math, division, or the associa	ative property to solve. (Use scratch paper if you like.)
	a. Is 12 a multiple of 3? Is 3	a factor of 12?
	b. Is 48 a multiple of 8? Is 48	B a factor of 8?
	c. Is 56 a multiple of 6? Is 6	a factor of 56?

4. Can a prime number be a multiple of any other number except itself? Explain why or why not.



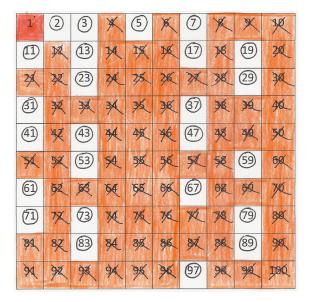
5. Follow the directions below.

1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

- a. Underline the multiples of 6. When a number is a multiple of 6, what are the possible values for the ones digit?
- b. Draw a square around the multiples of 4. Look at the multiples of 4 that have an odd number in the tens place. What values do they have in the ones place?
- c. Look at the multiples of 4 that have an even number in the tens place. What values do they have in the ones place? Do you think this pattern would continue with multiples of 4 that are larger than 100?
- d. Circle the multiples of 9. Choose one. What do you notice about the sum of the digits? Choose another one. What do you notice about the sum of the digits?



1. A student used the sieve of Eratosthenes to find all prime numbers less than 100. Create a step-by-step set of directions to show how it was completed. Use the word bank to help guide your thinking as you write the directions. Some words may be used just once, more than once, or not at all.



Wo	ord Bank
composite	cross out
number	shade
circle	X
multiple	prime

Directions for completing the sieve of Eratosthenes activity:





_	144		1 11 1			
')	What do a	all of the	numbers that are	Crossed (	aut have	in common y
۷.	vviiat ao t	411 OI UIC	Hullibels that are	CIUSSCUL	Juliave	

3. What do all of the circled numbers have in common?

4. There is one number that is neither crossed out nor circled. Why is it treated differently?





Lesson 25:

multiples.

Date \_\_\_\_\_

1. Draw place value disks to represent the following problems. Rewrite each in unit form and solve.

a.  $6 \div 3 =$ 

6 ones ÷ 3 = \_\_\_\_\_ones

b. 60 ÷ 3 = \_\_\_\_\_

6 tens ÷ 3 = \_\_\_\_\_

c. 600 ÷ 3 = \_\_\_\_\_

\_\_\_\_\_÷ 3 =\_\_\_\_\_

d. 6,000 ÷ 3 = \_\_\_\_

÷ 3 = \_\_\_\_\_

2. Draw place value disks to represent each problem. Rewrite each in unit form and solve.

a. 12 ÷ 4 = \_\_\_\_\_

12 ones ÷ 4 = \_\_\_\_\_ones

b. 120 ÷ 4 = \_\_\_\_\_

÷ 4 = \_\_\_\_\_

c. 1,200 ÷ 4 = \_\_\_\_\_

\_\_\_\_\_ ÷ 4 = \_\_\_\_\_



Lesson 26:

Divide multiples of 10, 100, and 1,000 by single-digit numbers.



3. Solve for the quotient. Rewrite each in unit form.

a.	800 ÷ 4 = 200	b. 900 ÷ 3 =	c. 400 ÷ 2 =	d. 300 ÷ 3 =
	8 hundreds ÷ 4 = 2 hundreds			
e.	200 ÷ 4 =	f. 160 ÷ 2 =	g. 400 ÷ 5 =	h. 300 ÷ 5 =
	20 tens ÷ 4 = tens			
i.	1,200 ÷ 3 =	j. 1,600 ÷ 4 =	k. 2,400 ÷ 4 =	I. 3,000 ÷ 5 =
	12 hundreds ÷ 3 = hundreds			

4. A fleet of 5 fire engines carries a total of 20,000 liters of water. If each truck holds the same amount of water, how many liters of water does each truck carry?

5.	Jamie drank 4 times as much juice as Brodie.	Jamie drank 280 milliliters of juice.	How much juice did
	Brodie drink?		

6. A diner sold \$2,400 worth of French fries in June, which was 4 times as much as was sold in May. How many dollars' worth of French fries were sold at the diner in May?

Na	me	Date	
1.	Divide. Use place value disks to model each	problem.	
	a. 346 ÷ 2		
	b. 528 ÷ 2		



Lesson 27:

Represent and solve division problems with up to a three-digit dividend numerically and with place value disks requiring decomposing a remainder in the hundreds place.



c. 516 ÷ 3	3	
d. 729÷3	3	
d. 723 · .		



Lesson 27:

Represent and solve division problems with up to a three-digit dividend numerically and with place value disks requiring decomposing a remainder in the hundreds place.



2.	Model using	place value	disks.	and record	using the	algorithm.

a.	648 ÷ 4 Disks	Algorithm
b.	755 ÷ 5 Disks	Algorithm
c.	964 ÷ 4 Disks	Algorithm



Lesson 27:

Represent and solve division problems with up to a three-digit dividend numerically and with place value disks requiring decomposing a remainder in the hundreds place.



Nar	me _		_		Date	
•	Divid	le. Check your woi	rk by multiplying. [	Draw disks on a place valu	e chart as needed.	
	a.	378 ÷ 2				
	b.	795 ÷ 3				
	c.	512 ÷ 4				



Lesson 28:

Represent and solve three-digit dividend division with divisors of 2, 3, 4, and 5 numerically.



d.	492 ÷ 4				
e.	539 ÷ 3				
f.	862 ÷ 5				



Lesson 28:

Represent and solve three-digit dividend division with divisors of 2, 3, 4, and 5 numerically.



g.	498 ÷ 3
h.	783 ÷ 5
i.	621 ÷ 4



Lesson 28:

Represent and solve three-digit dividend division with divisors of 2, 3, 4, and 5 numerically.



j.	531 ÷ 4

2. Selena's dog completed an obstacle course that was 932 meters long. There were 4 parts to the course, all equal in length. How long was 1 part of the course?



ame	Date	
Divide, and then check using multiplication.		
a. 2,464 ÷ 4		
b. 1,848 ÷ 3		
c. 9,426 ÷ 3		
c. 3, 120 · 3		



d.	6,587 ÷ 2
e.	5,445 ÷ 3
f.	5,425 ÷ 2



Lesson 29:

Represent numerically four-digit dividend division with divisors of 2, 3, 4, and 5, decomposing a remainder up to three times.



g.	8,467 ÷ 3
h.	8,456 ÷ 3
i.	4,937 ÷ 4



Lesson 29:

Represent numerically four-digit dividend division with divisors of 2, 3, 4, and 5, decomposing a remainder up to three times.



j.	6,173 ÷ 5

2. A truck has 4 crates of apples. Each crate has an equal number of apples. Altogether, the truck is carrying 1,728 apples. How many apples are in 3 crates?



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Divide. Check your solutions by multiplying.

1.  $409 \div 5$ 

2. 503 ÷ 2

3.  $831 \div 4$ 

4.  $602 \div 3$ 



5.  $720 \div 3$ 

6.  $6,250 \div 5$ 

7.  $2,060 \div 5$ 

9,031 ÷ 2



9.  $6,218 \div 4$ 

10. 8,000 ÷ 4



Lesson 30:

Solve division problems with a zero in the dividend or with a zero in  $% \left( 1\right) =\left( 1\right) \left( 1\right)$ the quotient.



Na	lame	Date	
	olve the following problems. Draw tape diagrams to he following problems.	elp you solve. Identify if the group size or the numbe	ŗ
1.	. 500 milliliters of juice was shared equally by 4 childr	en. How many milliliters of juice did each child get?	
2.	Kelly separated 618 cookies into baggies. Each bagg did Kelly make?	ie contained 3 cookies. How many baggies of cookie	:S
3.	. Jeff biked the same distance each day for 5 days. If he travel each day?	he traveled 350 miles altogether, how many miles di	d



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4.	A piece of ribbon 876 inches long was cut by a machine into 4-inch long strips to be made into bows.
	How many strips were cut?

5. Five Martians equally share 1,940 Groblarx fruits. How many Groblarx fruits will 3 of the Martians receive?



Lesson 31:

 $\label{thm:continuous} \mbox{Interpret division word problems as either } \mbox{\it number of groups } \mbox{\it unknown}$ or group size unknown.



us the following weekless. Draw tone diagrams to help you	
rtion of the tape diagram to represent that portion of the wh	solve. If there is a remainder, shade in a smandle.
Meneca bought a package of 435 party favors to give to the that she could give 9 party favors to each guest. How many	· · · · ·
4,000 pencils were donated to an elementary school. If 8 c many pencils did each class receive?	lassrooms shared the pencils equally, how
2,008 kilograms of potatoes were packed into sacks weighi packed?	ng 8 kilograms each. How many sacks were
	Meneca bought a package of 435 party favors to give to the that she could give 9 party favors to each guest. How many 4,000 pencils were donated to an elementary school. If 8 c many pencils did each class receive?





4.	A baker made 7 batches of muffins.	There was a total of 252 muffins.	If there was the same number of
	muffins in each batch, how many m	uffins were in a batch?	

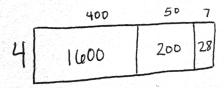
5. Samantha ran 3,003 meters in 7 days. If she ran the same distance each day, how far did Samantha run in 3 days?



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Name	Date

1. Arabelle solved the following division problem by drawing an area model.



- a. What division problem did she solve?
- b. Show a number bond to represent Arabelle's area model, and represent the total length using the distributive property.

2. a. Solve  $816 \div 4$  using the area model. There is no remainder in this problem.

b. Draw a number bond and use a written method to record your work from Part (a).



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3. a. Draw an area model to solve  $549 \div 3$ .

- b. Draw a number bond to represent this problem.
- c. Record your work using the long division algorithm.

4. a. Draw an area model to solve  $2,762 \div 2$ .

- b. Draw a number bond to represent this problem.
- c. Record your work using the long division algorithm.





Name	Date

- 1. Use the associative property to rewrite each expression. Solve using disks, and then complete the number sentences.
  - a.  $20 \times 34$ = (\_\_\_\_×10) × 34

=\_\_\_\_

hundreds	tens	ones

b.  $30 \times 34$ 

thousands	hundreds	tens	ones

c.  $30 \times 42$ 

thousands	hundreds	tens	ones



2. Use the associative property and place value disks to solve.

a.  $20 \times 16$ 

b.  $40 \times 32$ 

3. Use the associative property without place value disks to solve.

a. 30 × 21

b.  $60 \times 42$ 

4. Use the distributive property to solve the following. Distribute the second factor.

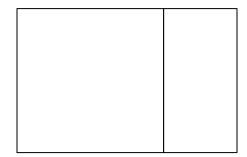
a.  $40 \times 43$ 

b.  $70 \times 23$ 

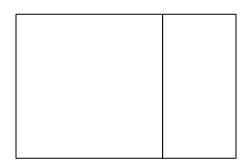
Name	Date	
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Use an area model to represent the following expressions. Then, record the partial products and solve.

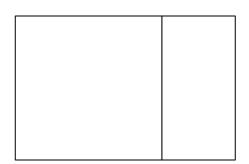
## 1. 30 × 17



## 2. $40 \times 58$



## 3. $50 \times 38$



Draw an area model to represent the following expressions. Then, record the partial products vertically and solve.

4.  $60 \times 19$ 

5. 20 × 44

Visualize the area model, and solve the following expressions numerically.

6. 20 × 88

7. 30 × 88

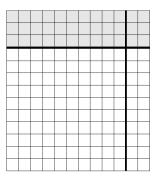
8.  $70 \times 47$ 

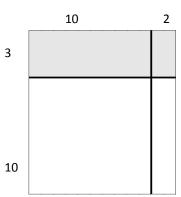
9.  $80 \times 65$ 



Name	Date	
_		

1. a. In each of the two models pictured below, write the expressions that determine the area of each of the four smaller rectangles.

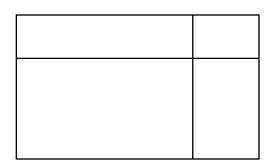




b. Using the distributive property, rewrite the area of the large rectangle as the sum of the areas of the four smaller rectangles. Express first in number form, and then read in unit form.

Use an area model to represent the following expression. Record the partial products and solve.

2.  $17 \times 34$ 



Draw an area model to represent the following expressions. Record the partial products vertically and solve.

3.  $45 \times 18$ 

4.  $45 \times 19$ 

Visualize the area model and solve the following numerically using four partial products. (You may sketch an area model if it helps.)

5. 12 × 47

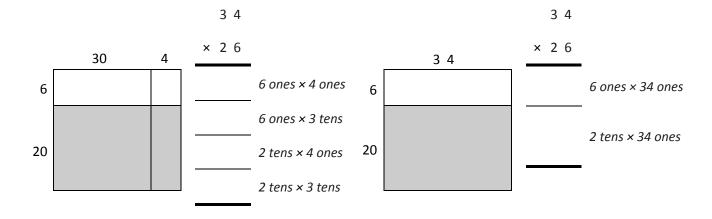
6. 23 × 93

7. 23 × 11

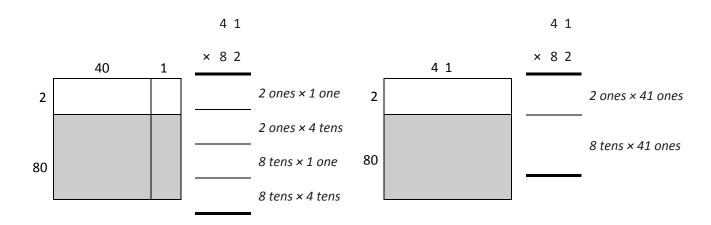
8.  $23 \times 22$ 



1. Solve 26 × 34 using 4 partial products and 2 partial products. Remember to think in terms of units as you solve. Write an expression to find the area of each smaller rectangle in the area model.



2. Solve using 4 partial products and 2 partial products. Remember to think in terms of units as you solve. Write an expression to find the area of each smaller rectangle in the area model.



3. Solve 52 × 26 using 2 partial products and an area model. Match each partial product to its area on the model.

4. Solve the following using 2 partial products. Visualize the area model to help you.

a.	6	8

c. 1 6

d. 5 4

Name \_\_\_\_\_

Date \_\_\_\_\_

4 3

1. Express  $26 \times 43$  as two partial products using the distributive property. Solve.

	43
6	
20	

26 × 43 = (\_\_\_\_\_ forty-threes) + (\_\_\_\_ forty-threes)

× 26	<u>_</u>
	6 ×
	20 ×

2. Express  $47 \times 63$  as two partial products using the distributive property. Solve.

	63
7	
40	
+0	

47 × 63 = (\_\_\_\_\_ sixty-threes) + (\_\_\_\_\_ sixty-threes)

× 47	_
	×
	- ×
	^

6 3

3. Express  $54 \times 67$  as two partial products using the distributive property. Solve.

54 × 67 = ( × ) + ( × )

	6 /	
×	5 4	_
		×
		×

4. Solve the following using two partial products.

5 2 3 4

5. Solve using the multiplication algorithm.

8 6 5 6

6.  $54 \times 52$ 7.  $44 \times 76$  8.  $63 \times 63$ 

9.  $68 \times 79$ 



Lesson 38:

 $\label{thm:continuity} Transition from four partial products to the standard algorithm for two-digit by two-digit multiplication.$ 

